Gravitational Wave Astrophysics Pablo Marchant

Part 4: Parameter estimation of a compact object coalescence

Image credit: LIGO/T. Pyle

Today 12/5 19/5

- History of the field
- Types of detectors
- Types of sources
- Current state of the field
	- Future advancements

- Ground based interferometers

- Production of GWs from compact object binaries

- Parameter estimation from observed compact object coalescences

- Astrophysics of observed GW sources

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GW sources

From data to binary properties

How do we move from an observed waveform to a set of properties in a compact binary coalescence?

Detectors are noisy!

GW150914, discovery paper Physical Review Letters 116, 061102 (2016)

Time (s)

GW150914, discovery paper Physical Review Letters 116, 061102 (2016) GW170817 (binary NS), discovery paper

Detectors are noisy!

Physical Review Letters 119,161101 (2017)

Time (seconds)

GW150914, discovery paper Physical Review Letters 116, 061102 (2016) GW170817 (binary NS), discovery paper

Detectors are noisy!

Physical Review Letters 119,161101 (2017)

Actual data for GW170817 showed a very

strong glitch in LIGO-Livingston!

Detectors are noisy!

Signal in an interferometer will always be a combination of an actual GW signal and the interferometer noise.

$s(t) = n(t) + h(t)$

Sudden events of noise in the detector can be interpreted as fake signals. There is a significant effort to characterize not just the steady well behaved noise spectrum but also these "glitches"

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'teardrop' shape

One example of a common glitch in LIGO data

https://www.zooniverse.org/projects/ zooniverse/gravity-spy

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Network of interferometers is critical to distinguish real from artificial signals!

'teardrop' shape

For each template $h(t)$ and for the strain data from a single detector $s(t)$, the analysis calculates the square of the matched-filter SNR defined by [12]

$$
\rho^2(t) \equiv \frac{1}{\langle h|h\rangle} |\langle s|h\rangle(t)|^2,
$$

where the correlation is defined by

$$
\langle s|h\rangle(t) = 4 \int_0^\infty \frac{\tilde{s}(f)\tilde{h}^*(f)}{S_n(f)} e^{2\pi i f}
$$

where $\tilde{s}(f)$ is the Fourier transform of the time domain quantity $s(t)$ given by

$$
\tilde{s}(f) = \int_{-\infty}^{\infty} s(t) e^{-2\pi i f t} dt.
$$

The quantity $S_n(|f|)$ is the one-sided average power spectral density of the detector noise, which is re-calculated every 2048 s (in contrast to the fixed spectrum used in template bank construction). Calculation of the matched-filter SNR in the frequency domain allows the use of the computationally efficient Fast Fourier Transform [80, 81]. The square of the matched-filter SNR in Eq. (1) is normalized by

$$
\langle h|h\rangle = 4 \int_0^\infty \frac{\tilde{h}(f)\tilde{h}^*(f)}{S_n(f)} df
$$

so that its mean value is 2, if $s(t)$ contains only stationary noise $[82]$.

GW150914, CBC search paper Phys. Rev. D 93, 122003 (2016)

 (1)

 ${}^t \, \mathrm{d} f$, (2)

 (3)

 (4)

CBC stands for compact binary coalescence. In this case we know from first principles what a signal should look like and we can search through the data for it. The method used for this is called matched filtering.

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Signal is further weighted by additional criteria that checks for the resemblance of a signal to a CBC,

 $\hat{\rho} = \begin{cases} \rho / [(1 + (\chi_r^2)^3)/2]^{\frac{1}{6}}, & \text{if } \chi_r^2 > 1, \\ \rho, & \text{if } \chi_r^2 \leq 1. \end{cases}$

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A final "detection statistic" is built by averaging the weighted SNR between detectors. For two LIGO detectors this is:

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 $\hat{\rho}_c = \sqrt{\hat{\rho}_c}$, Hanford + $\hat{\rho}_c$, Livingston

Matched filtering for GW151226 (binary BH merger). Credit: A. Nitz https://www.youtube.com/watch?v=bBBDR5jf9oU

Matched filtering

Signal-to-noise Ratio (SNR) 15 10 5 -5 -10 -15

https://www.youtube.com/watch?v=bBBDR5jf9oU

Exercise 1

$s(t) = f(t - t_0), h(t) = f(t)$

$$
\propto \tilde{s}(f)\tilde{h}^*(f)e^{2\pi i f t}df
$$

Let's make a simple illustration of how matched filtering does this shift in time to compare to a template. Imagine a "signal" and a "template" given by:

The template is just the same as the signal but shifted in time. What value of t gives the maximum for the following integral?

Matched filtering (GW150914)

GW150914, CBC search paper, Phys. Rev. D 93, 122003 (2016)

to the data yields one template with a high detection statistic. Is this a spurious result?

The rate of high significance events can be determined from the data itself. With a network of detectors, artificially long stretches of data can be produced by time-shifting them with respect to each other.

Matched filtering (GW150914)

Time-shifting produces artificial high significance events when the signal of GW150914 matches a glitch.

This analysis provides a measure of the false-alarm rate of a detection.

GW150914, CBC search paper, Phys. Rev. D 93, 122003 (2016)

Matched filtering (GW150914)

GWTC-1: A GRAVITATIONAL-WAVE TRANSIENT CATALOG ... PHYS. REV. X 9, 031040 (2019)

Search results for the 11 GW events. We report a false-alarm rate for each search that found a given event; otherwise, we TABLE I. display \cdots . The network SNR for the two matched-filter searches is that of the template ranked highest by that search, which is not necessarily the template with the highest SNR. Moreover, the network SNR is the quadrature sum of the detectors coincident in the highest-ranked trigger; in some cases, only two detectors contribute, even if all three are

Inferring source parameters

After identifying a signal, what information can be extracted from it?

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Inferring source parameters

 $masses(m_1, m_2)$, spins (\vec{S}_1, \vec{S}_2) , tidal deformability $(\widetilde{\Lambda})$, eccentricity

Spin magnitudes and lorientations, eccentricity, ... tell us something about how these binaries formed

Extrinsic parameters:

time (t_c) , reference phase (φ_c) , sky position (α, δ) , distance (d_L) , orbital orientation (θ_{1n}, ψ) ,

Credit: LIGO/Virgo

Credit: Alan J. Weistein

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Credit: LIGO/Virgo

determine its properties. Credit: Alan J. Weistein Once a signal is identified an extensive search is made against waveforms to

What we have seen in the previous class:

 $\mathcal{M} = \frac{c^3}{G} \left(\frac{5}{96} \pi^{-8/3} f^{-11/3} \dot{f} \right)^{3/5}$ $h \propto \frac{\mathcal{M}^{3/5}}{r}$

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In practice we cannot ignore cosmology, and we observe a redshifted frequency:

 $\mathcal{M}(1+z) = \frac{c^3}{G} \left(\frac{5}{96} \pi^{-8/3} f_{\rm obs}^{-11/3} \dot{f}_{\rm obs} \right)^{3/5}$ $h \propto \frac{\mathcal{M}^{3/5}}{d\tau}$

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A distance measurement requires a cosmological model or an independent redshift measurement!

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Exercise 2

Derive the expression for the redshifted mass.

 $\mathcal{M}(1+z) = \frac{c^3}{G} \left(\frac{5}{96} \pi^{-8/3} f_{\rm obs}^{-11/3} \dot{f}_{\rm obs} \right)^{3/5}$

2 LIGO/University of Oregon/Ben Farr

Chirp mass

Less massive binaries are observable for more cycles

time observable (seconds)

https://www.youtube.com/watch?v=I1Ut6h6PkOw

Chirp mass

Chirp mass

Chirp mass

Chirp mass

 $m_1 \,[\mathrm{M}_\odot]$ GW170817, chirp mass determined with a precision of 0.001 solar masses

Binary black shorter lives on band, leading to less constrained chirp masses.

 (2016)

Results from LIGO's O1

Signal Units Computer Computer between mass ratio and control and con
The control and the number of cycles a merging compact object Using the formula for the time to merger, estimate has before coalescing by taking the product of the merger time and the frequency at 10 Hz. How many cycles would a source with a chirp mass of a solar mass have? For which chirp mass you'd expect to have about a single cycle before merger?

Exercise 3

After the chirp mass, the best constrained quantities are usually the mass ratio and the effective spin:

$q=m_2/m_1$

 $m_1\chi_1+m_2\chi_2$ Xef m_1+m_2

Where the chi give the components of the spin aligned with the orbital plane.

These two parameters have a degenerate effect on the waveform, though this degeneracy can be broken with sufficiently accurate observations.

Mass ratio and spin

Results from LIGO's O1 Physical Review X 6,041015 (2016)

Localization

Prospects for localization of sources Living Reviews in Relativity volume 21, Article number: 3 (2018)

more than 100 square degrees.

Localization of sources comes mostly from triangulation. Except for a couple of sources, uncertainty in location is

Localization

Article number: 3 (2018)

credit: LIGO-Virgo collaboration

And from all this, catalogues!

B.P. ABBOTT et al.

remnant discussed in Sec. VE.

TABLE III. Selected source parameters of the 11 confident detections. We report median values with 90% credible intervals that include statistical errors and systematic errors from averaging the results of two waveform models for BBHs. For GW170817, credible intervals and statistical errors are shown for IMRPhenomPv2NRT with a low spin prior, while the sky area is computed from TaylorF2 samples. The redshift for NGC 4993 from Ref. [94] and its associated uncertainties are used to calculate source-frame masses for GW170817. For BBH events, the redshift is calculated from the luminosity distance and assumed cosmology as discussed in Appendix B. The columns show source-frame component masses m_i and chirp mass M, dimensionless effective aligned spin χ_{eff} , final source-frame mass M_f , final spin a_f , radiated energy E_{rad} , peak luminosity l_{peak} , luminosity distance d_L , redshift z, and sky localization $\Delta\Omega$. The sky localization is the area of the 90% credible region. For GW170817, we give conservative bounds on parameters of the final

PHYS. REV. X 9, 031040 (2019)

Want to know more?

 \mathbb{O} A https://astro-gr.org/online-course-gravitational-waves/

Me Contact Home

Pygmalion \bullet OpenBS

8 - LIGO Data Analysis

- 1. The context: LIG
- 2. LIGO data attrib
- 3. Some signal proc
- 4. Optimal filtering
- 5. Stochastic backg
- 6. Hypothesis testing: maximum likelihood; Baysean statistics; false alarm probability compared with detection probability
- 7. Searching for (transient) bursts of GW's
- 8. Analysis of data from a network of detectors

Astro-GR course has some lectures on LIGO data analysis. But better to use more up to date info!

Lecturer Albert Lazzarini: "LIGO Data Analysis (1/2)"

Lecturer Albert Lazzarini: "LIGO Data Analysis (2/2)"

Collisions \blacktriangledown Workshops \blacktriangledown Par

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Presentations from open data workshops of the LVC are available online. workshop1 and workshop2 avalable also!

Want to know more?

A https://www.gw-openscience.org/s/workshop3/

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Gravitational-Wave Open Data Workshop #3

Advanced LIGO and Advanced Virgo are now observing the gravitational-wave sky with unprecedented sensitivity. To date, there have been over 50 potential gravitational-wave transients observed, and planned detector upgrades are likely to accelerate the pace of discovery in the coming years. This new window on the universe is providing insights on a range of topics, including compact body populations, cosmology, and fundamental physics.

LIGO and Virgo strain data from past observation runs and data snippets around discoveries are made publicly available at gw-openscience.org, along with associated software libraries. The LIGO and Virgo collaborations are hosting an Open Data Workshop to acilitate working with these data products. This workshop is the third edition of a series that began in 2018. It is intended for scientists and students who wish to learn about using gravitational-wave data and software in order to conduct research of their own. The workshop will provide a mixture of lecture style presentations and hands-on programming exercises, using publicly available gravitational-wave data and specialized software tools.

Want to know more?

Living Rev. Relativity, 12 , (2009) , 2 http://www.livingreviews.org/lrr-2009-2

Physics, Astrophysics and Cosmology with Gravitational Waves

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> Living Reviews in Relativity ISSN 1433-8351

> > Accepted on 29 January 2009 Published on 4 March 2009

Abstract

Gravitational wave detectors are already operating at interesting sensitivity levels, and they have an upgrade path that should result in secure detections by 2014. We review the physics of gravitational waves, how they interact with detectors (bars and interferometers), and how these detectors operate. We study the most likely sources of gravitational waves and review the data analysis methods that are used to extract their signals from detector noise. Then we consider the consequences of gravitational wave detections and observations for physics, astrophysics, and cosmology.

Really a good review for both parts of today's lecture.

Want to know more?

OPEN ACCESS IOP Publishing

Class. Quantum Grav. 37 (2020) 055002 (54pp)

A guide to LIGO-Virgo detector noise and extraction of transient gravitational-wave signals

Up to date overview of the methods being used for signal processing.

Classical and Quantum Gravity

https://doi.org/10.1088/1361-6382/ab685e